

# Multi-sampled Photon Differentials

Incorporating the View Ray Differential in the Radiance Estimate

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# Outline

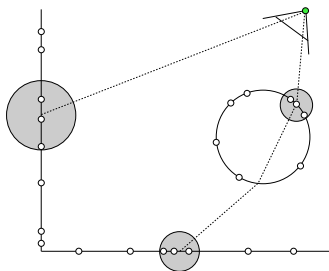
- ▶ What is photon mapping?
- ▶ What are photon differentials?
- ▶ Why consider the view ray differential?
- ▶ Introducing two different approaches:
  - ▶ Coplanar intersection-weighted photon differentials
  - ▶ Multi-sampled photon differentials
- ▶ Results

# What is photon mapping?

- ▶ Global illumination algorithm by Henrik Wann Jensen
- ▶ Solves the rendering equation in discrete form:

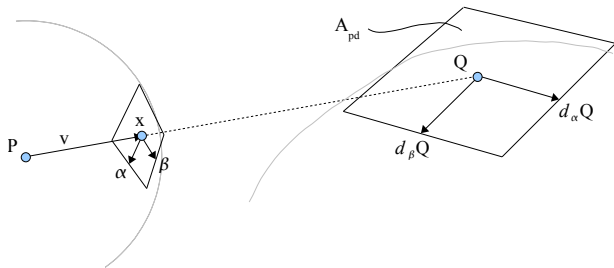
$$L_r(x, \omega) \approx \sum_{p=1}^k f_r(x, \omega_p, \omega) \frac{\Delta\Phi_p(x, \omega_p)}{\Delta A} K(\|x_p - x\|)$$

- ▶ Algorithm is divided into two stages:
  - ▶ Photon tracing
  - ▶ Rendering



# What are photon differentials? (1/2)

- ▶ Extension of photon mapping proposed by Schjøth et al.
- ▶ Observation:
  - ▶ Finite number of emitted photons  $\rightarrow$  each photon can be regarded as the center of a beam with size and shape
- ▶ Associates photons with *ray differentials* ( $dV$ ,  $dP$ )
- ▶ Differential position vectors approximate footprint of beam on intersecting surfaces



## What are photon differentials? (2/2)

- ▶ Can trace ray differentials alongside original ray by evaluating the differentials of the trace operations – example for transfer:

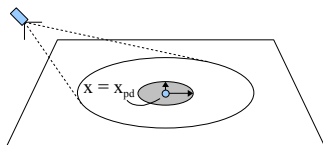
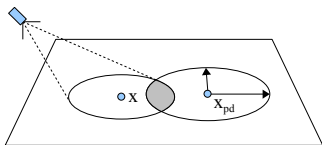
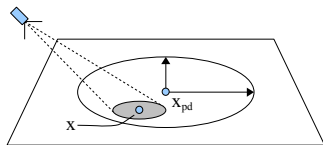
$$\begin{aligned}Q &= P + sV \\dQ &= dP + (ds)V + sdV\end{aligned}$$

- ▶ Schjøth et al. use the extra information inherent in the footprints to rewrite the radiance estimate:

$$L_r(x, \omega) \approx \sum_{pd=1}^k f_r(x, \omega_{pd}, \omega) \frac{\Phi_{pd}}{A_{pd}} K(\|M_{pd}(x - x_{pd})\|)$$

- ▶  $M_{pd}$  takes relative sampling point  $x - x_{pd}$  into filter space
- ▶ Filter space resembles an ellipsoid in world space
- ▶ Better at preserving features than regular photon mapping

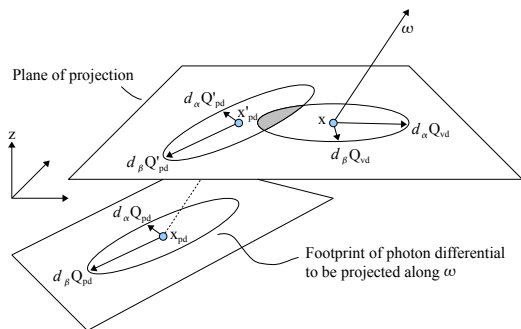
## Why consider the view ray differential?



- ▶ Should be possible to increase accuracy without tracing more view rays or increasing resolution of photon map

# Coplanar intersection-weighted photon differentials (1/2)

- ▶ Idea:
  - ▶ Compute intersection explicitly
  - ▶ Problem depends on how the footprints are interpreted
- ▶ Approximate by intersection of coplanar convex geometry:
  - ▶ Project footprints into common plane, rotate into 2D
  - ▶ Reconstruct as convex polygons to compute 2D intersection



## Coplanar intersection-weighted photon differentials (2/2)

- ▶ Intersection polygon  $C_{vd \cap pd}$  yields:
  - ▶  $w_{vd \cap pd}$  – coverage of intersection along current view ray
  - ▶  $x_{vd \cap pd}$  – approximate centroid of intersection (unprojected)
- ▶ These can be incorporated in the radiance estimate as follows:

$$L_r(x, \omega) \approx \sum_{pd=1}^k f_r(x, \omega_{pd}, \omega) \frac{\Phi_{pd}}{A_{pd}} K(\|M_{pd}(x_{vd \cap pd} - x_{pd})\|) w_{vd \cap pd}$$

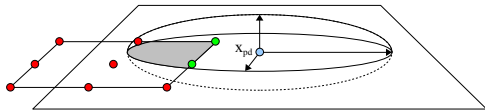
- ▶ Potential contribution of photon differential is scaled by coverage
- ▶  $K$  is evaluated in filter space transformation of  $x_{vd \cap pd}$ , not  $x$
- ▶ Successfully incorporates the view ray differential, but performance is lacking → prompts alternative approach



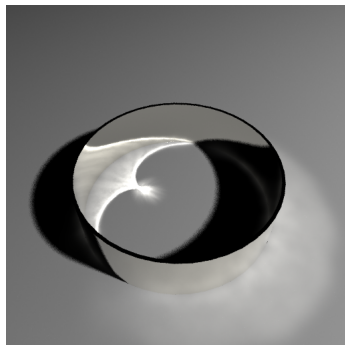
# Multi-sampled photon differentials

- ▶ Idea:
  - ▶ Do not compute the intersection explicitly, but sample the photon differential in multiple places, averaging the results
  - ▶ Use the view ray differential to define the sample distribution
- ▶ Letting  $X$  denote the set of  $N \times N$  sampling points, the radiance estimate can be written:

$$L_r(x, \omega) \approx \sum_{pd=1}^k f_r(x, \omega_{pd}, \omega) \frac{\Phi_{pd}}{A_{pd}} \left( \frac{1}{N^2} \sum_{i=1}^{N^2} K(\|M_{pd}(X_i - x_{pd})\|) \right)$$

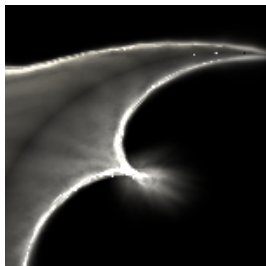


## Results (1/3)

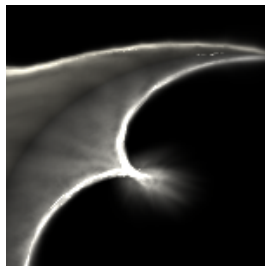


- ▶ Simple test case; the clearly defined contour of the caustic should provoke undersampling artefacts
- ▶ 120000 photon differentials, of which 20000 are caustic
- ▶  $k = 50$

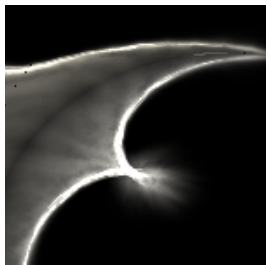
## Results (2/3)



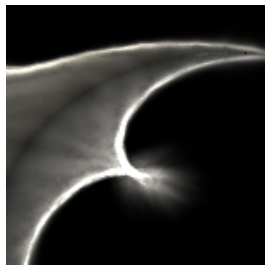
(a) Regular,  $1 \times 1$  rays/pixel



(b) Regular,  $3 \times 3$  rays/pixel



(c) Coplanar intersection-w.



(d) Multi-sampled,  $8 \times 8$

## Results (3/3)

Method	Rendering time in seconds
Regular, $1 \times 1$ view rays/pixel	20.637
Regular, $3 \times 3$ view rays/pixel	183.255
Coplanar intersection-weighted	380.045
Multi-sampled, $8 \times 8$ sampling points	63.671

- ▶ Increasing number of view rays/pixel results in linear increase in rendering time  $\rightarrow$  expected
- ▶ Coplanar intersection-weighted photon differentials does not perform well enough to be worth it over tracing more view rays per pixel
- ▶ Multi-sampled photon differentials performs well; three times faster than tracing more view rays per pixel, and the results are practically free of visible artefacts

That's it

Questions?